

# Latex Films

Dow Chemical Project

Jason Crowley, David Lehtihet

Andres Jaramillo-Botero and William A Goddard III

9-2-2011

# Outline

Thermodynamics as a function of water content  
(continued)

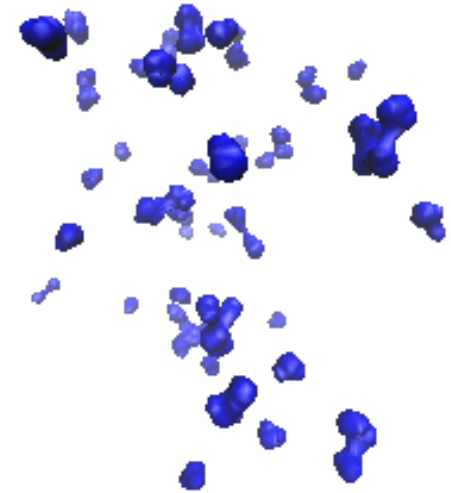
# Solvated Hydrophobic Polymer

- Equilibrate 40 wt% structure
- Remove water molecules at random to get 30, 25, 20, 15, 10, 5, 4, 3, 2, 1%
- Equilibration: CED as before, 1 ns NPT to finish
- Take snapshots once energy equilibrated. 5 snapshots (one every ~100ps)
- 2PT analysis on each snapshot for thermodynamics

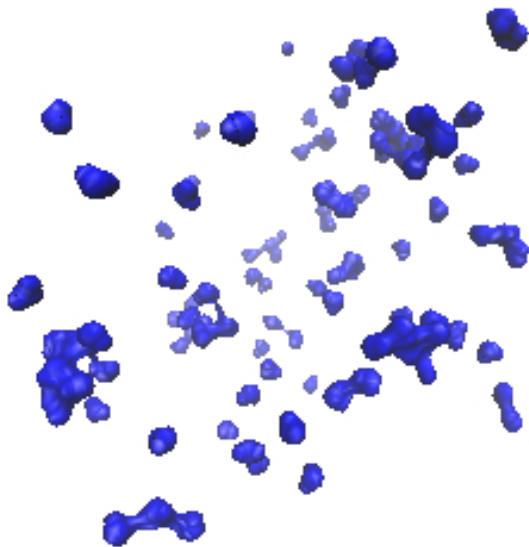
# Water Molecules Represented as Solid Surfaces



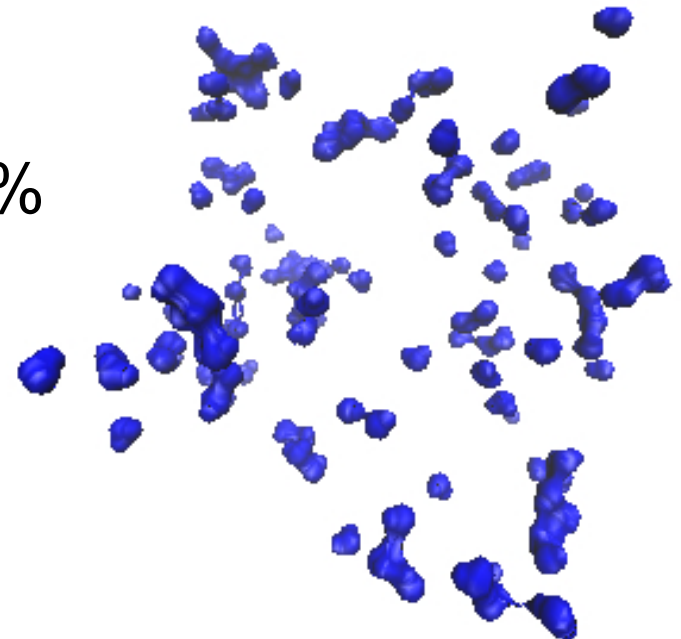
1 %



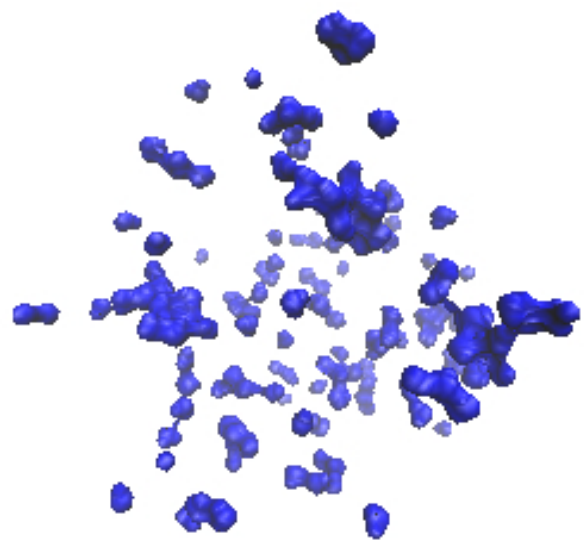
2%



3%

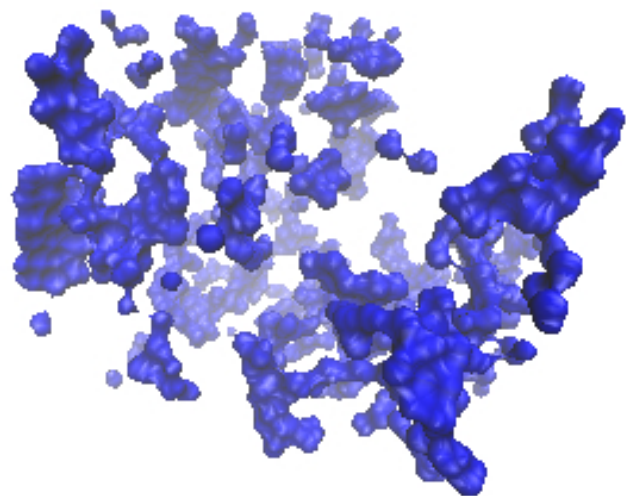
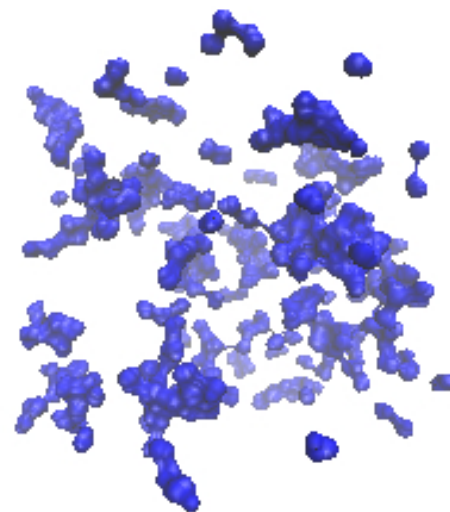


4%



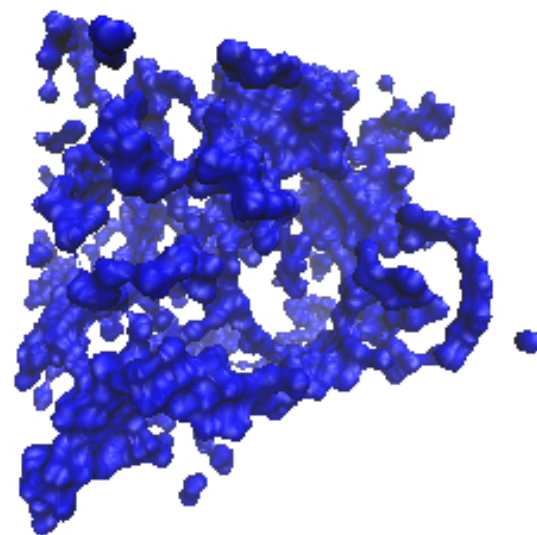
5%

10%

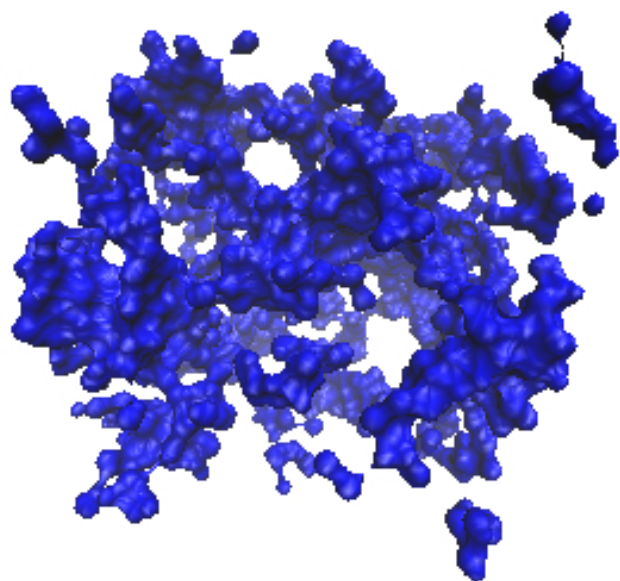


15%

20%

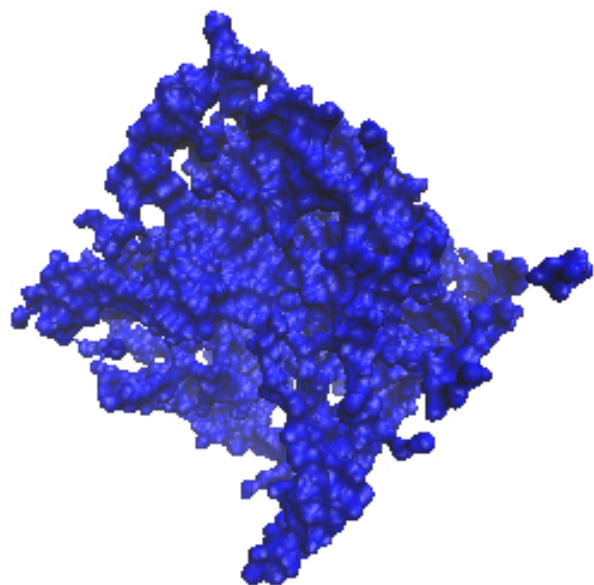
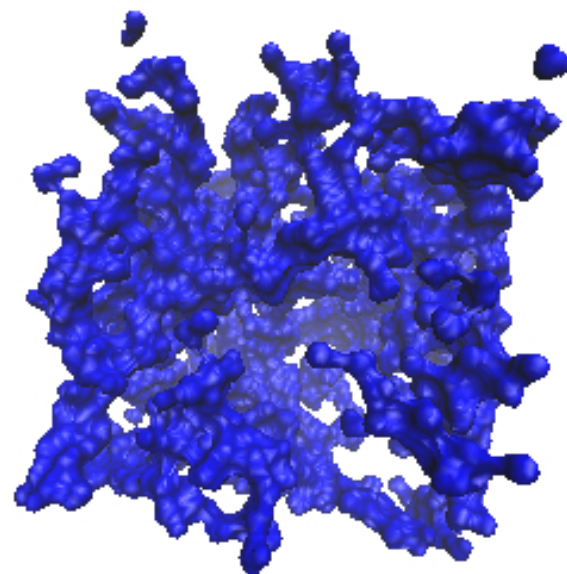


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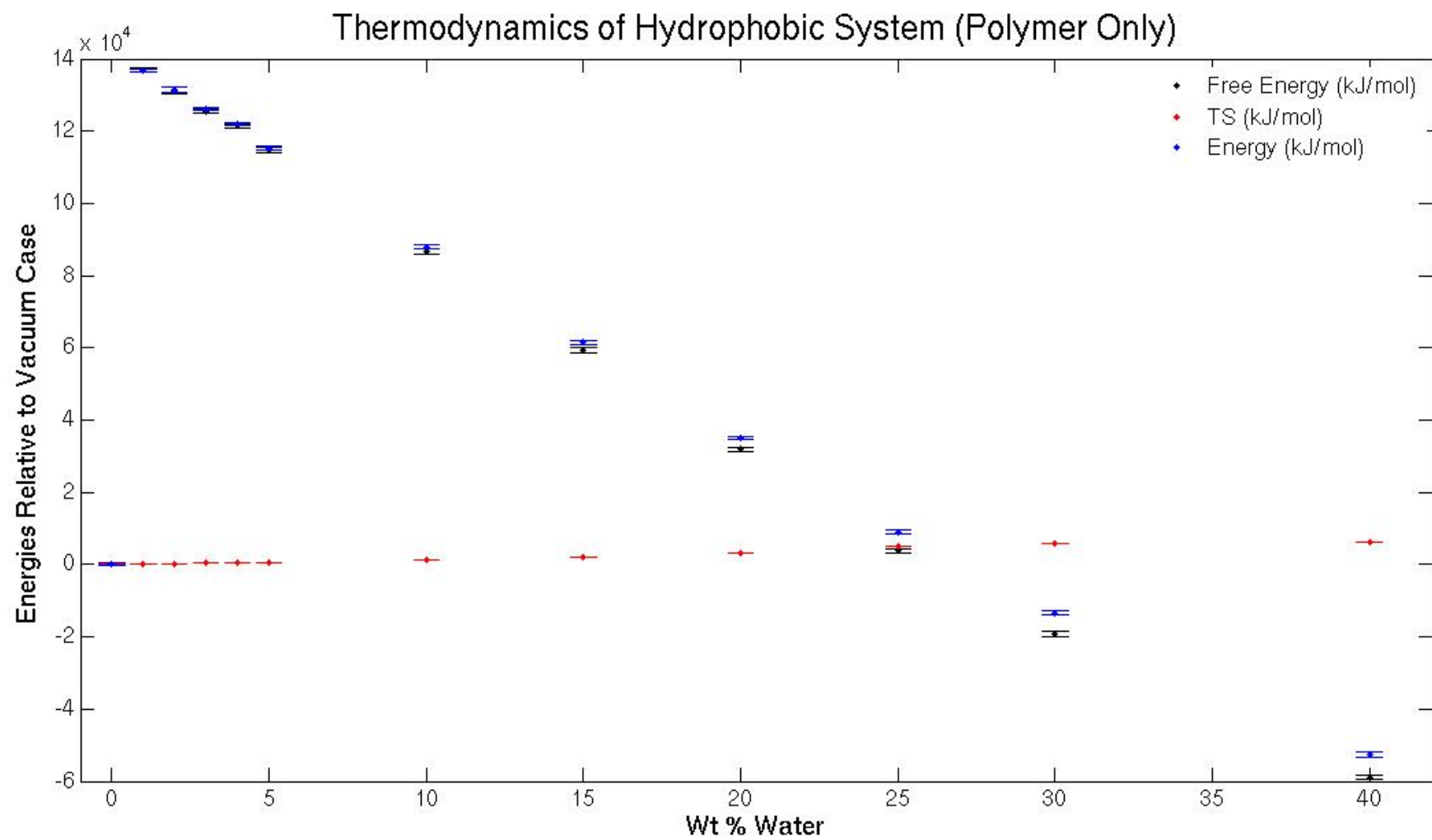


25%

30%

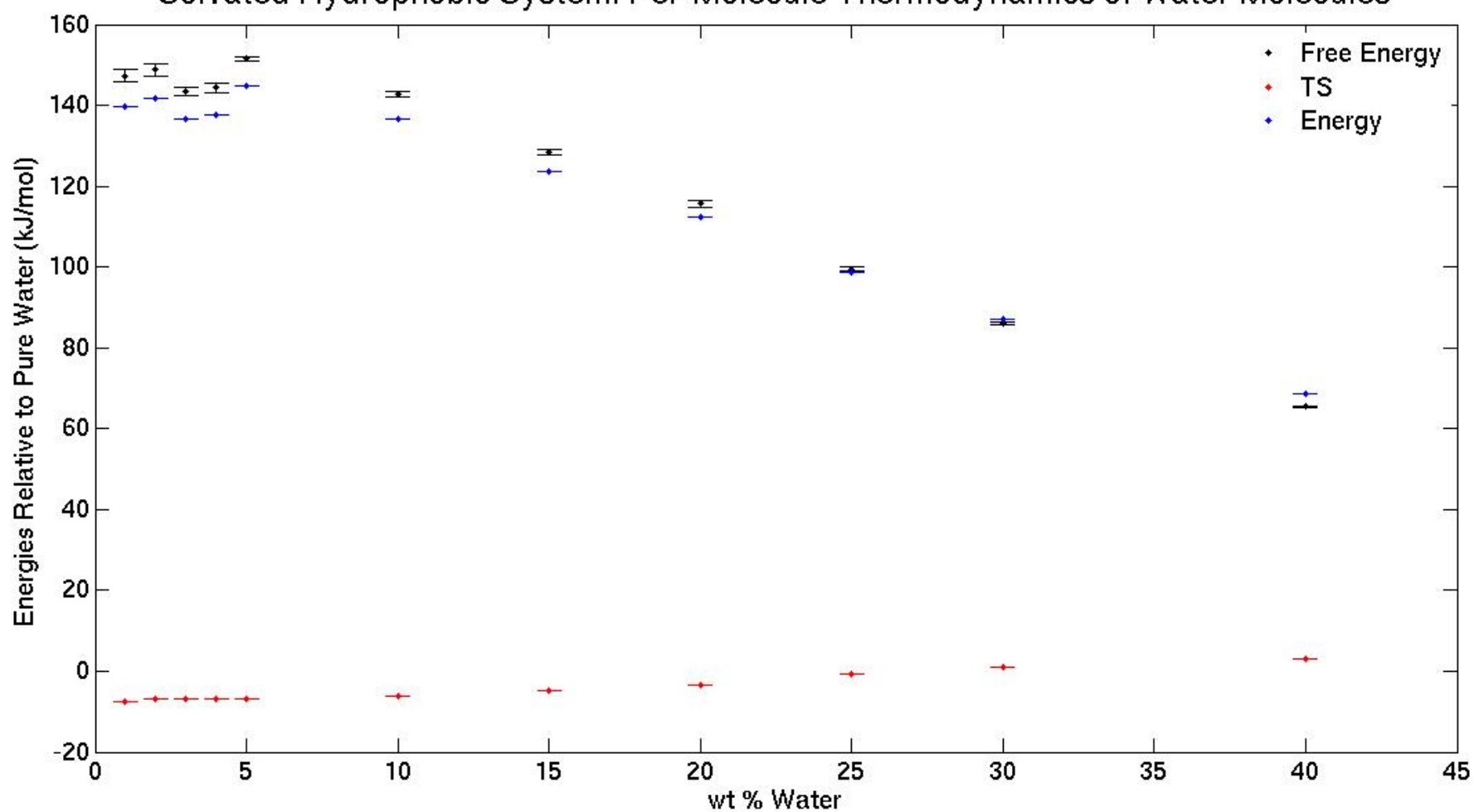


40%

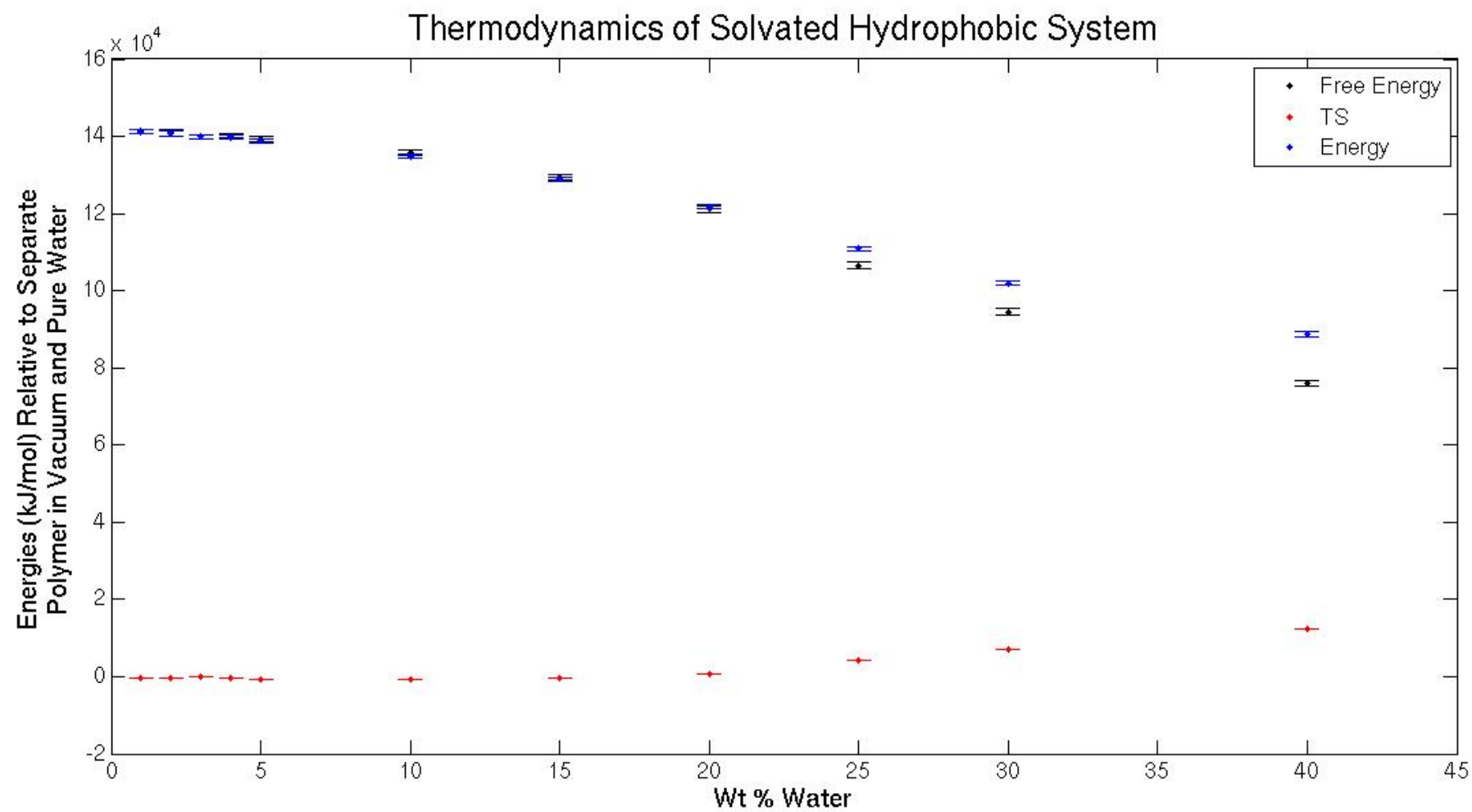


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# Solvated Hydrophobic System: Per-Molecule Thermodynamics of Water Molecules

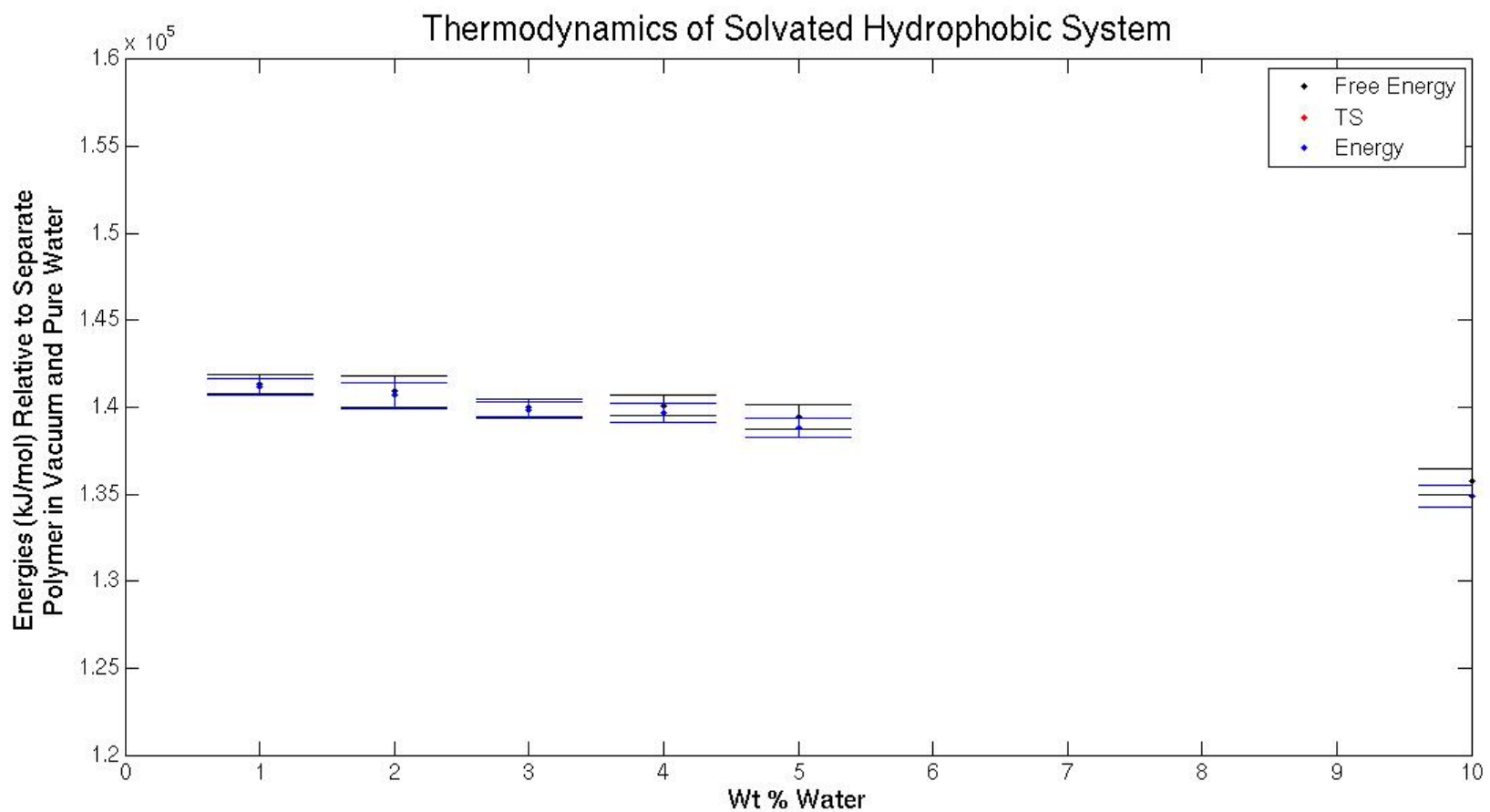






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# Same Figure, Zoomed in on Energy



# Solvated Hydrophilic Polymer

For the data plotted here:

Hydrophilic System Composition

DREIDING Polymer, F3C Water

Lennard-Jones, fixed partial charge, hydrogen-bonding between MMA\* and water

2PT data gathered for 20ps at 4fs intervals, NVT @ 300K and 1 g/cc

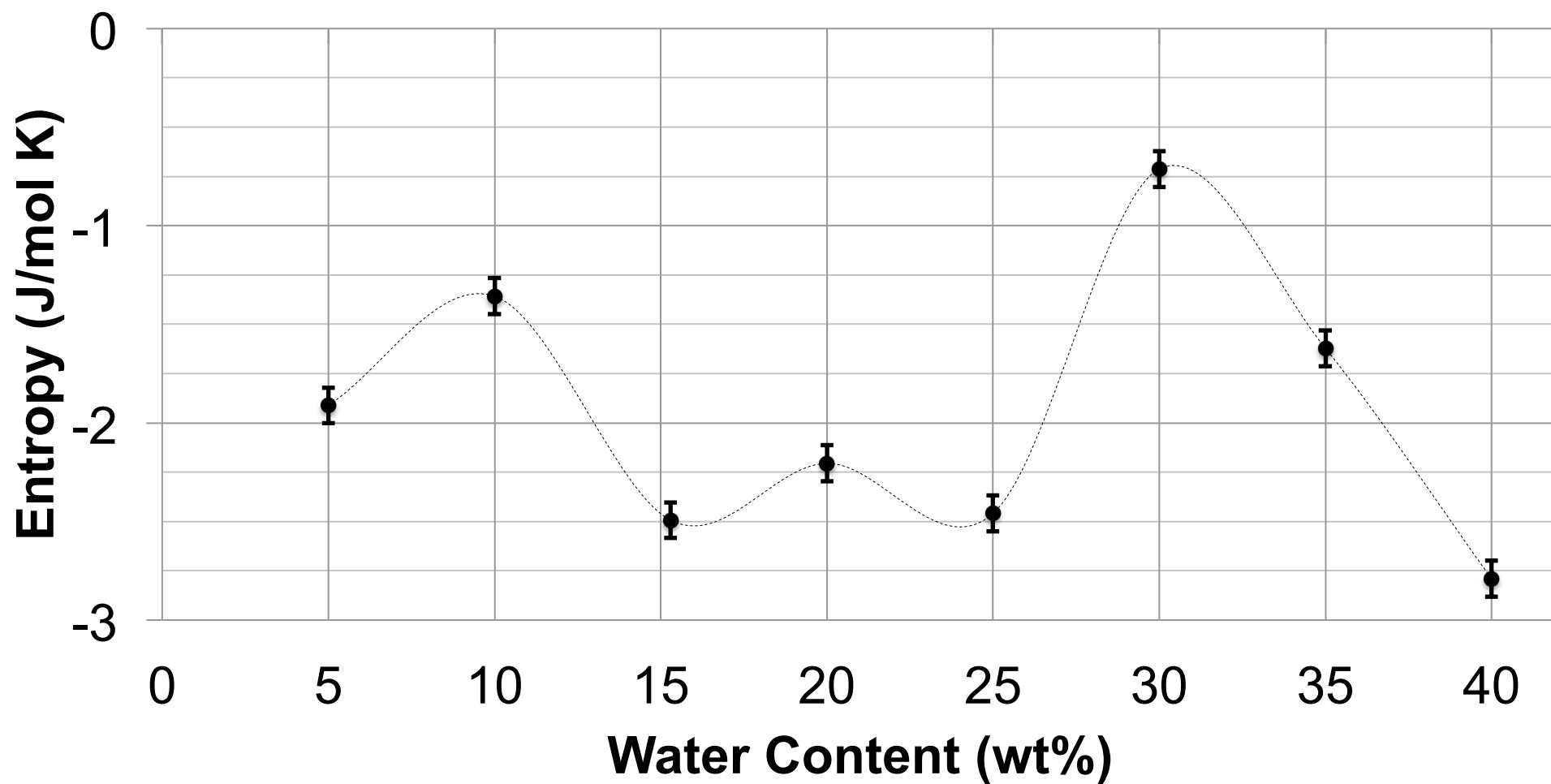
9163 polymer atoms

**Entropy Reference** – Bulk Water (F3C => 62.18 J/mol K), Vacuum Polymer

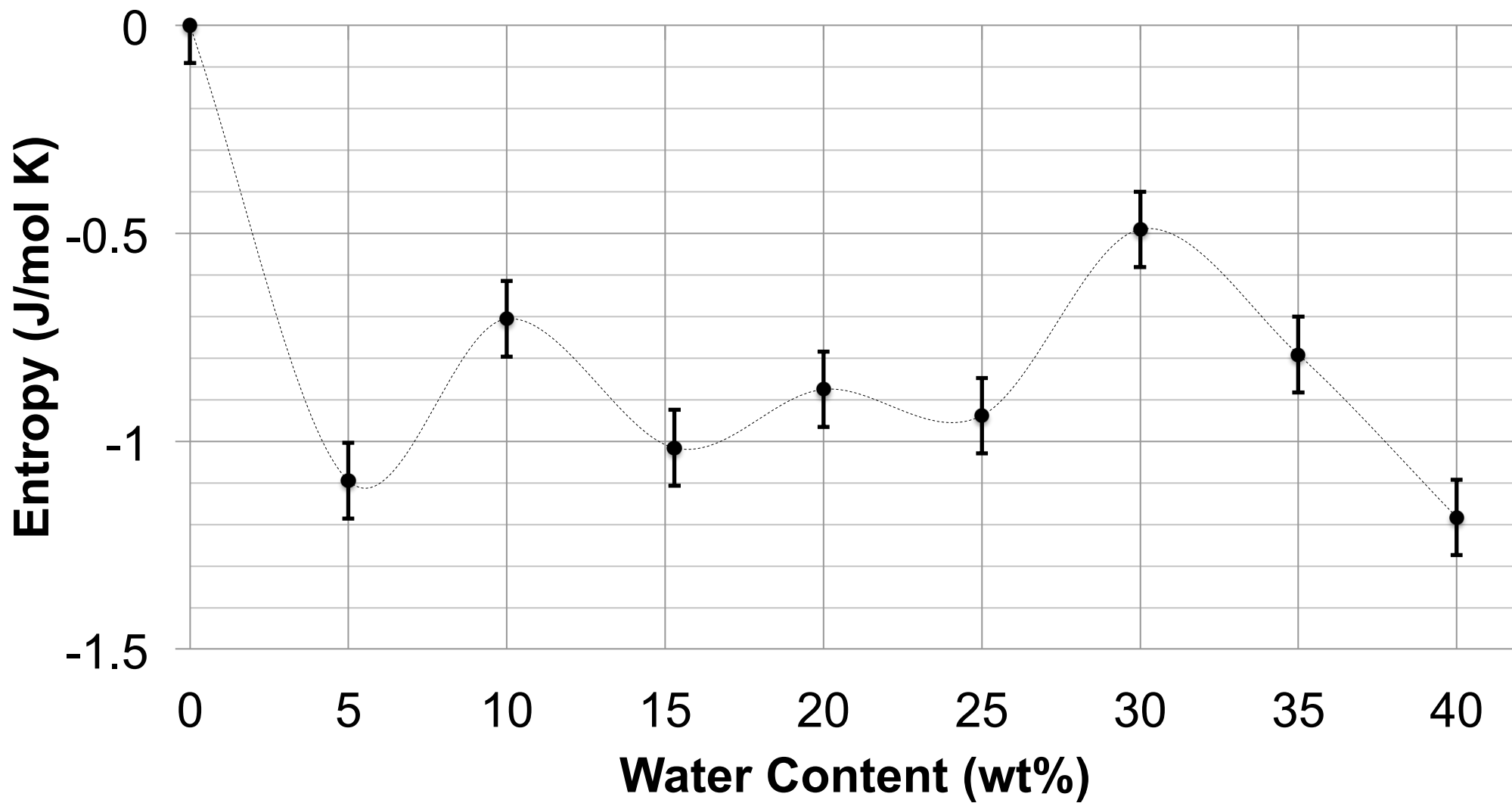
**Internal Energy Reference** – Bulk Water (F3C => -9.6 kcal/mol [-40.1664kJ/mol]),  
Vacuum Polymer

**Free Energy** =  $H - T \cdot S$

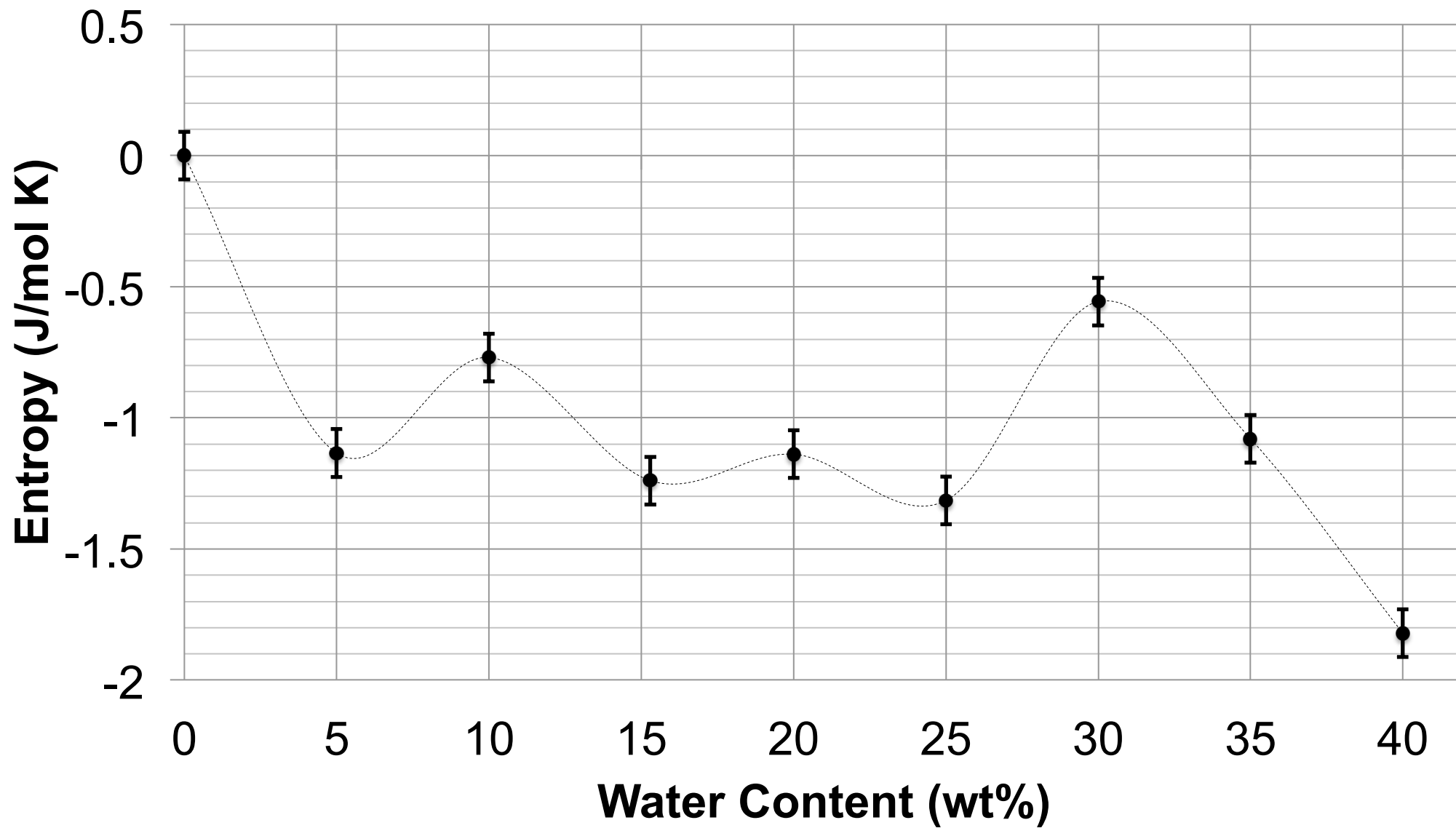
## Water Entropy, Per Atom - Hydrophilic System (1g/cc)



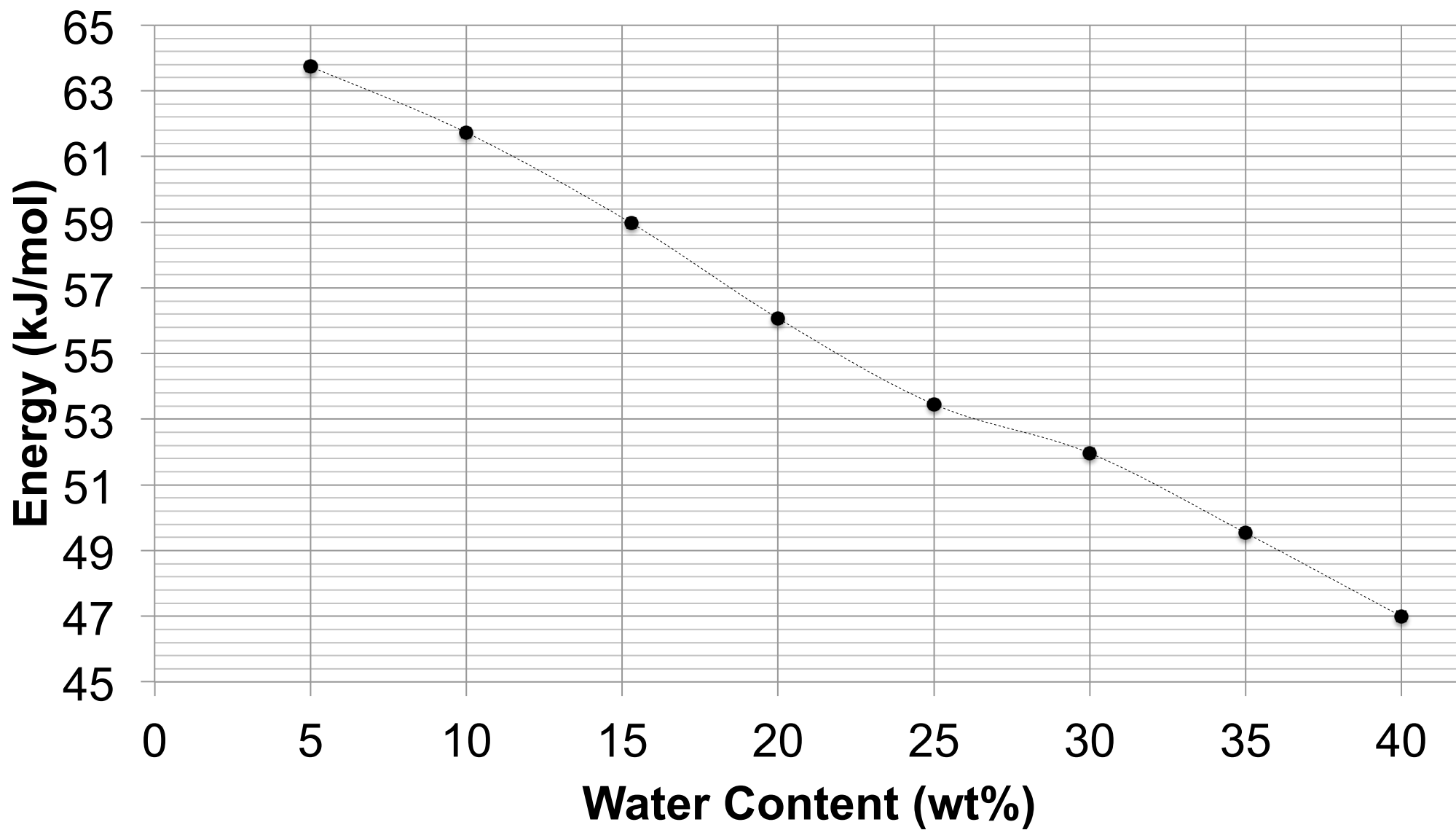
# Polymer Entropy, Per Atom - Hydrophilic System (1g/cc)



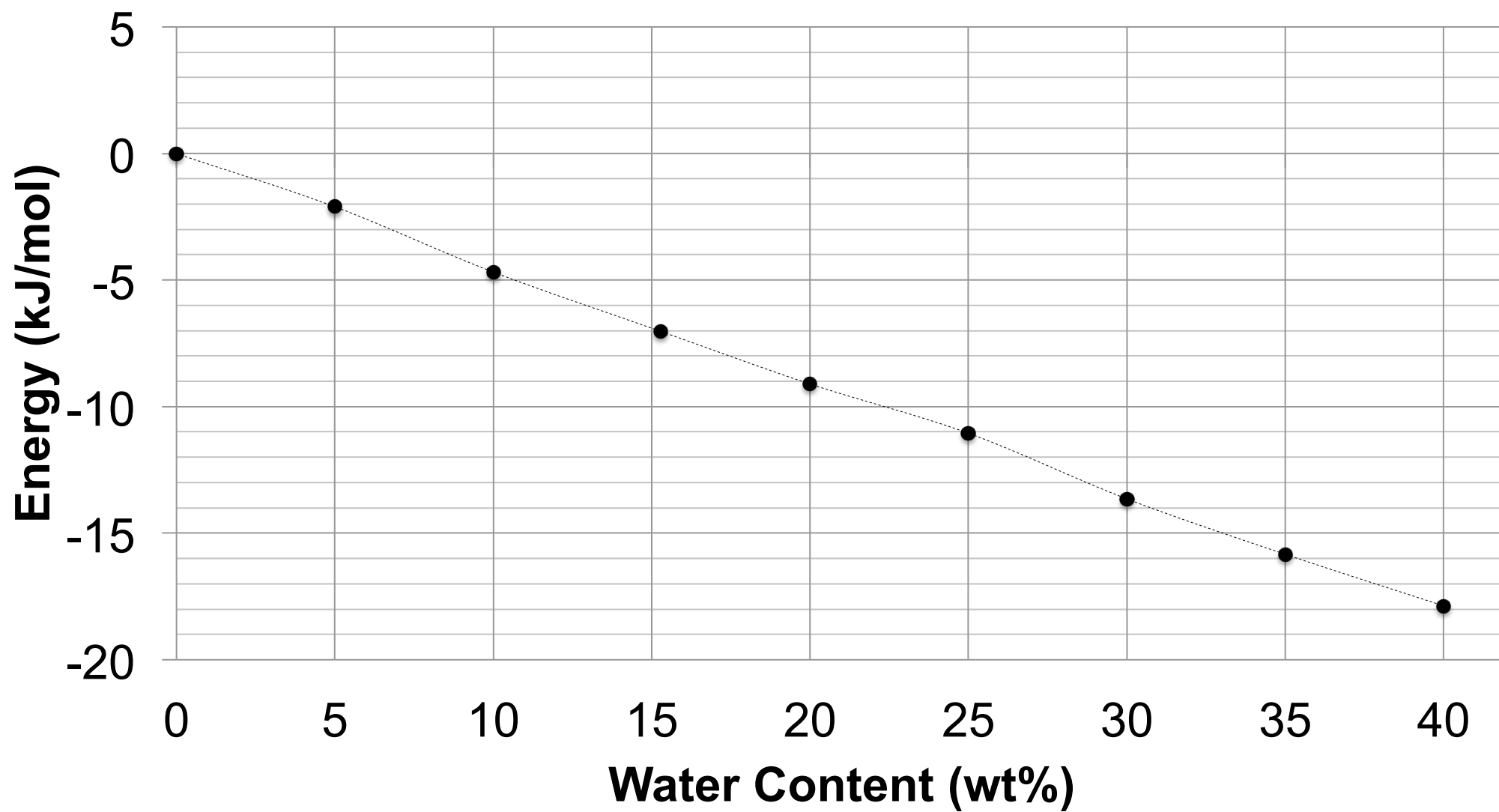
## Total Entropy, Per Atom - Hydrophilic System (1g/cc)



## Water Enthalpy, Per Atom - Hydrophilic System (1g/cc)

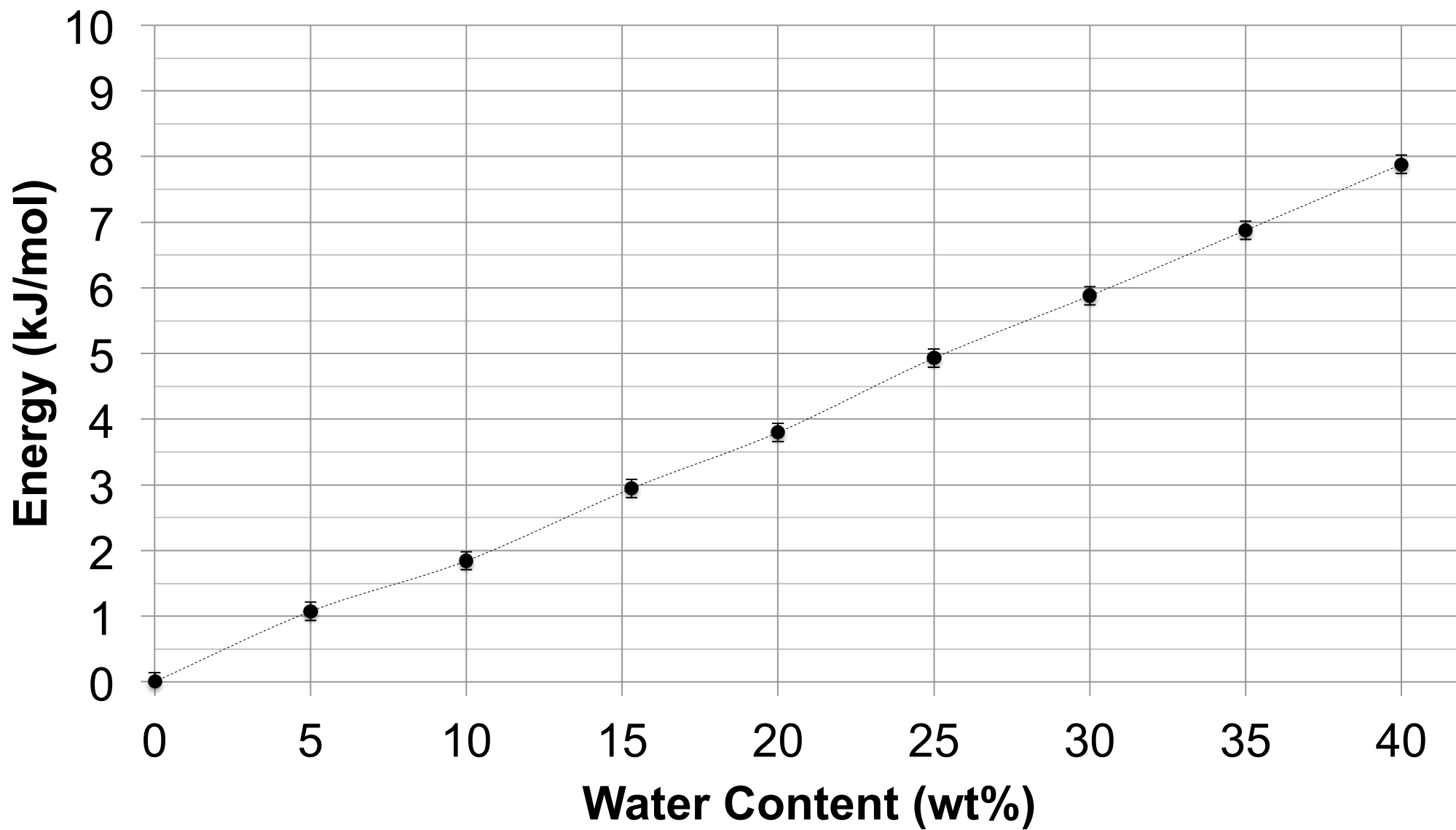


## Polymer Enthalpy, Per Atom - Hydrophilic System (1g/cc)

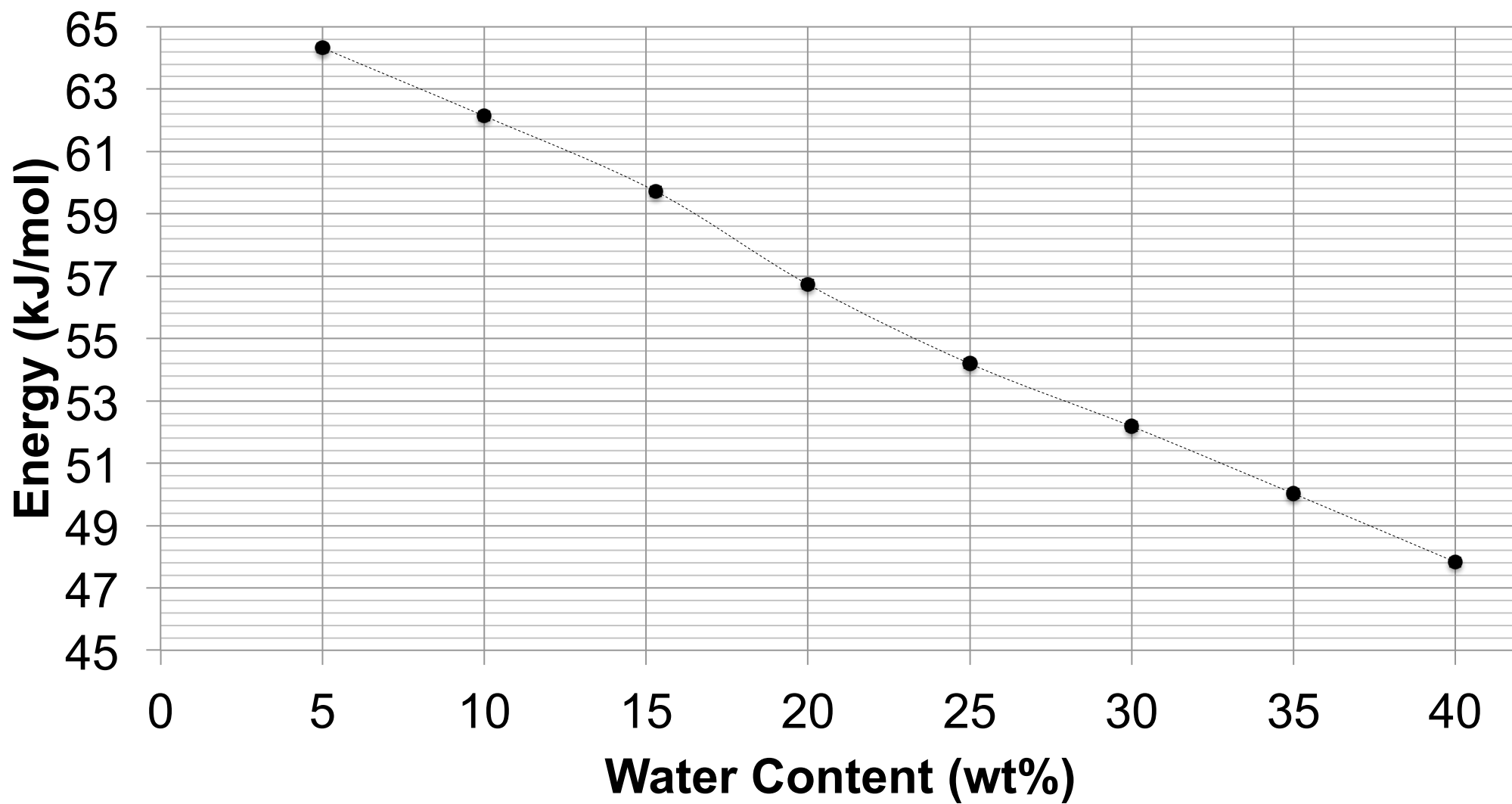




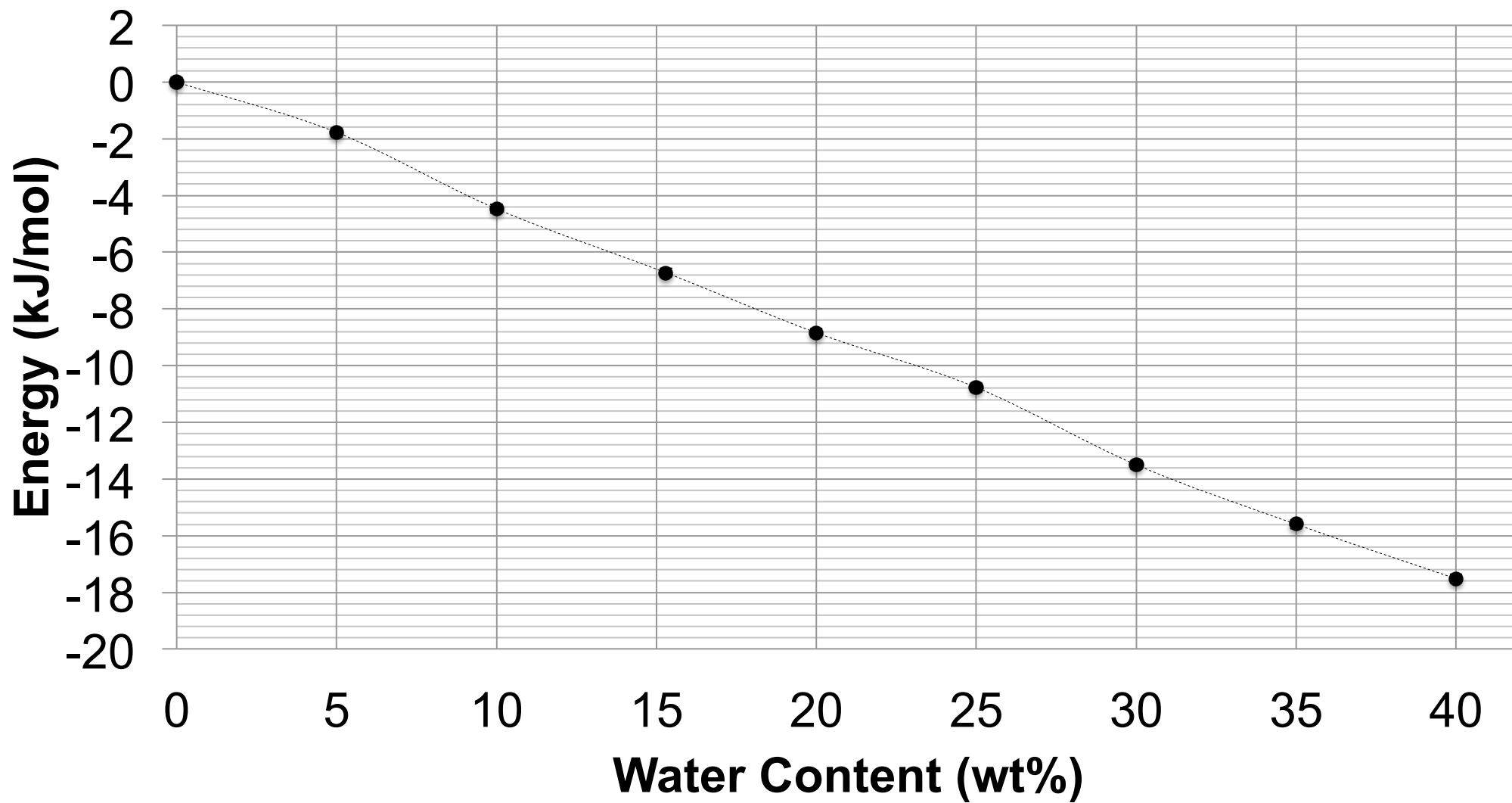
## Total Enthalpy, Per Atom - Hydrophilic System (1g/cc)



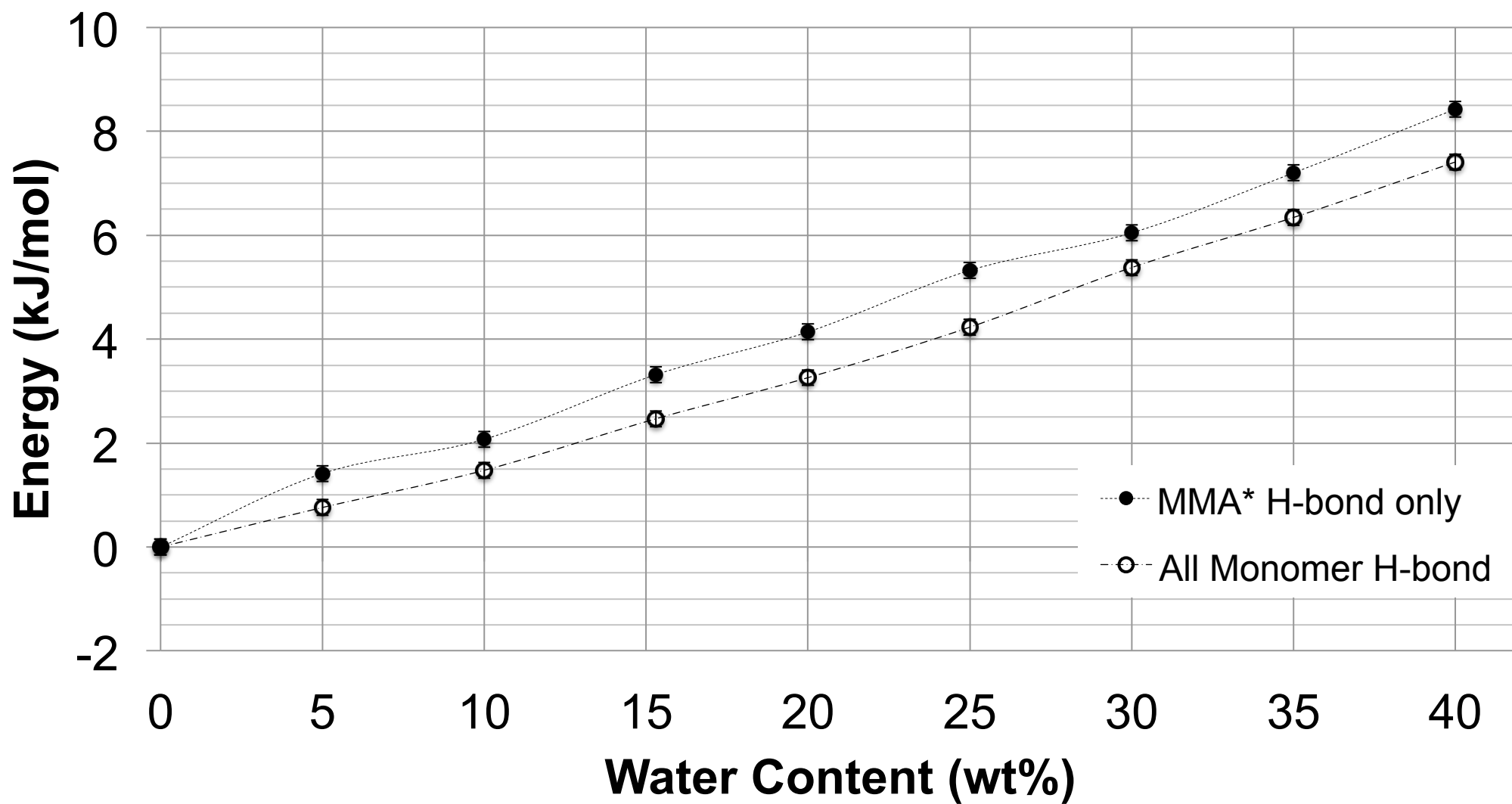
# Water Free Energy, Per Atom - Hydrophilic System (1g/cc)



## Polymer Free Energy, Per Atom - Hydrophilic System (1g/cc)



# Total Free Energy, Per Atom - Hydrophilic System (1g/cc)



## Contributions to Thermodynamic Properties:

| 40wt% Water | Polymer (%) | Water (%) |
|-------------|-------------|-----------|
| Entropy     | 42.5        | 57.5      |
| Enthalpy    | 58.7        | 41.3      |
| Energy      | 60.6        | 39.4      |

| 20wt% Water | Polymer (%) | Water (%) |
|-------------|-------------|-----------|
| Entropy     | 68.8        | 31.2      |
| Enthalpy    | 79.6        | 20.4      |
| Energy      | 80.4        | 19.6      |

Traditional

Entropy-based

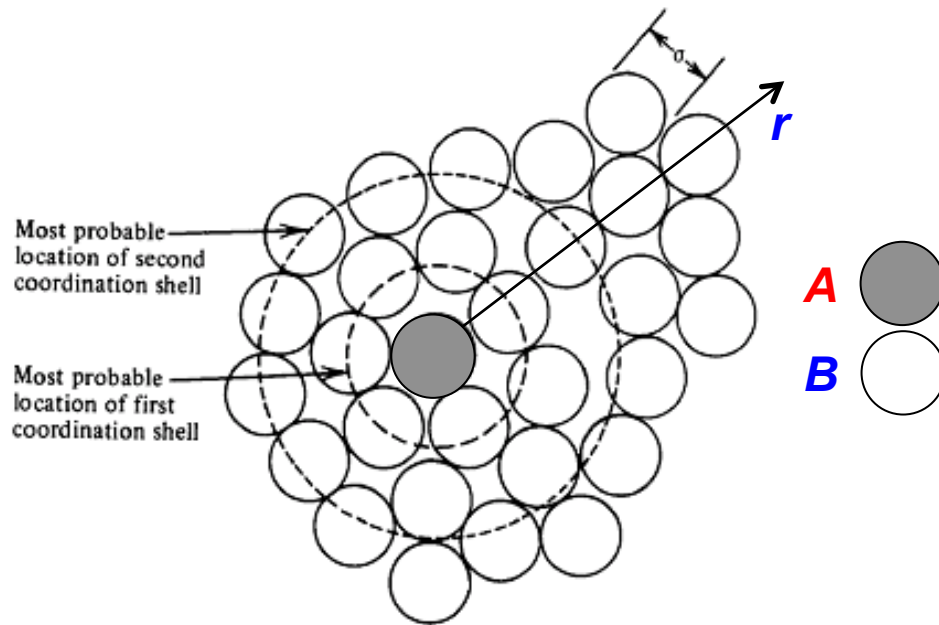
**SWELLING**

# Future Approaches: Pair Correlation Function

## Pair correlation function (PCF)

$$g_{A-B}(r) = \left( \frac{n_B}{4\pi r^2 \Delta r} \right) / \left( \frac{N_B}{V} \right)$$

$n_B$  is the number of particle B located at the distance  $r$  in a shell of thickness from particle A,  $N_B$  is the number of B particles in the system, and  $V$  is the total volume of the system.



PCF is probability density (or distribution density) of finding B molecule around A molecule at a distance  $r$ .

We expect:

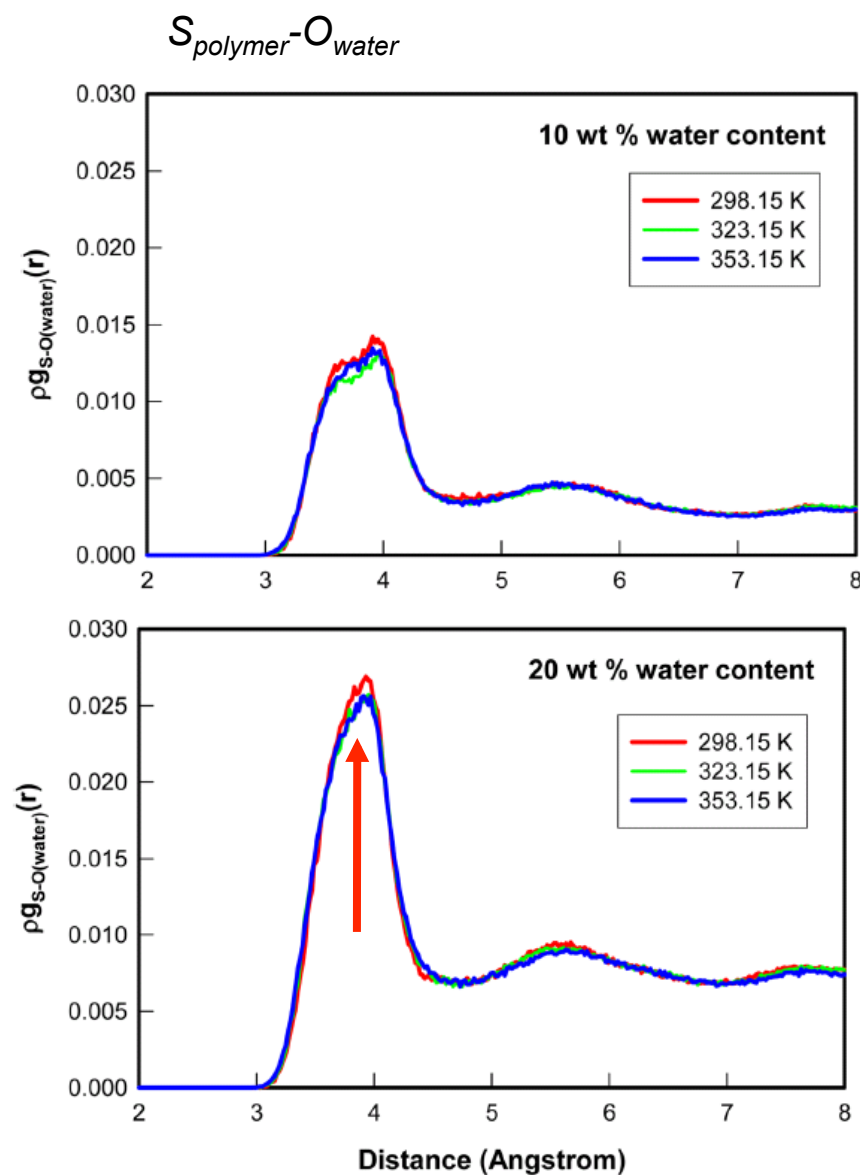
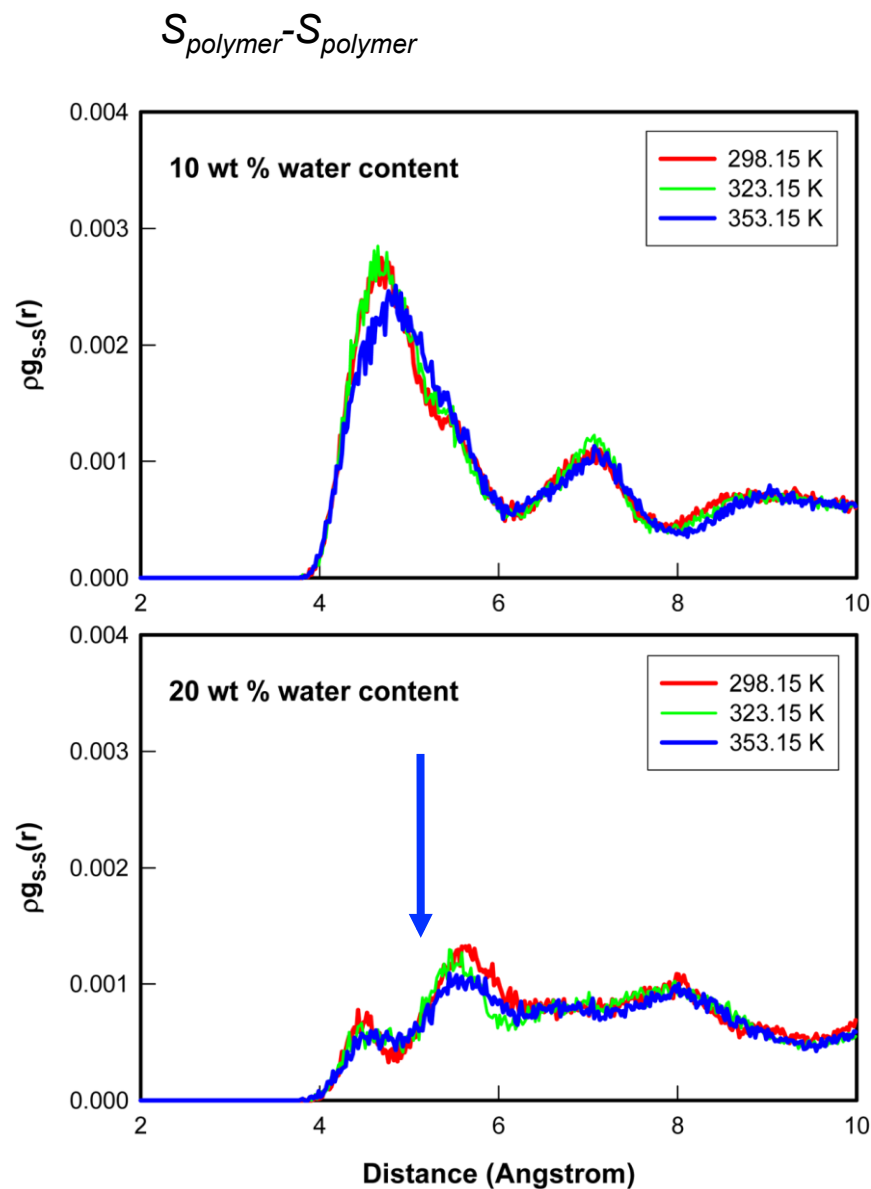
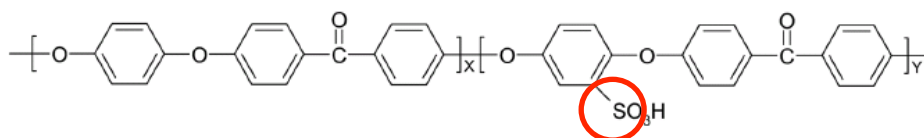
As increasing water contents,

Polymer-polymer PCF → **decrease** (due to swelling of the system)

Polymer-water PCF → **increase** (due to high water content)

# Future Approaches: Pair Correlation Function

## Case Study: Fuel Cell Membrane



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# Future Approaches: Mean Square Displacement

## Mean Square Displacement (MSD)

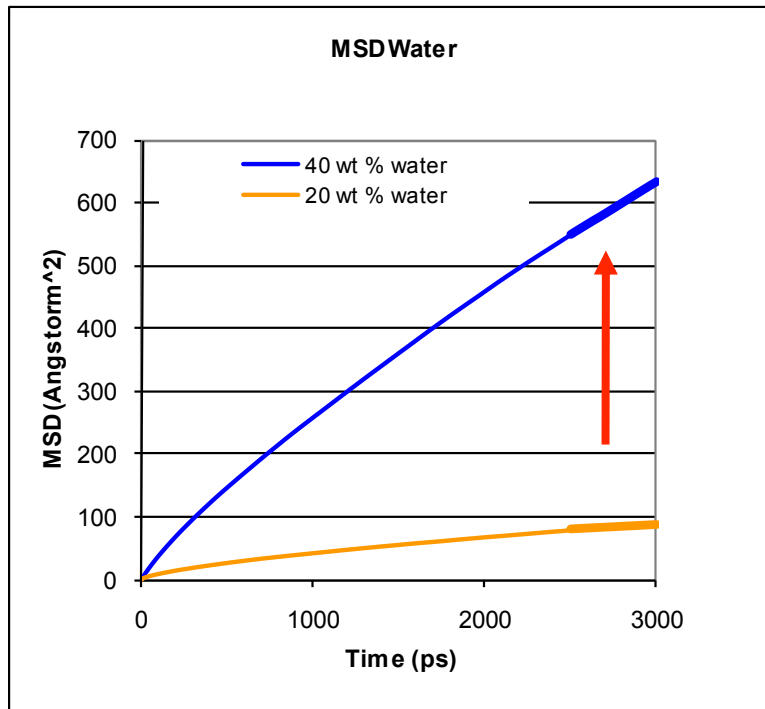
$$D = \lim_{t \rightarrow \infty} \frac{1}{6t} \left\langle (r(t) - r(0))^2 \right\rangle$$

$r(t)$  and  $r(0)$  are the positions of the target molecules at a time,  $t$ , greater than 0 and at  $t = 0$ , respectively

Diffusion coefficient can be determined by MSD of the target molecules.

We expect:

As increasing water contents, MSD of water → **increase** (due to swelling, free water > bound water)



## Case Study: Hydrogel

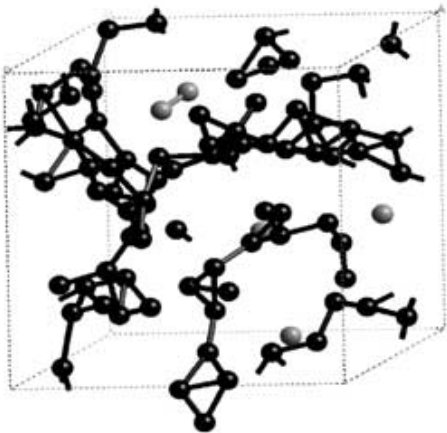
Diffusion coefficients of water ( $10^{-5}$  cm<sup>2</sup>/s) in hydrogel:

0.03 (20 wt %) → 0.28 (40 wt %)

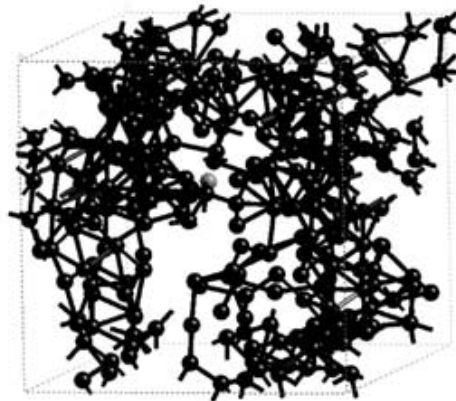
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# *Future Approaches: Percolation of water*

## **percolated water**



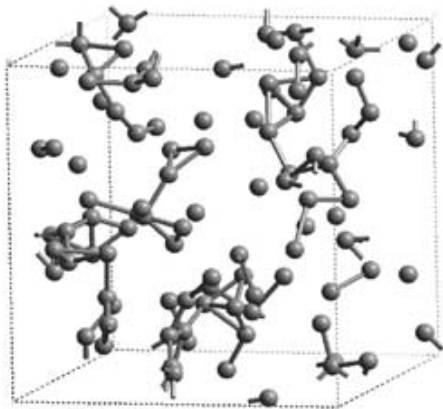
**18% water**



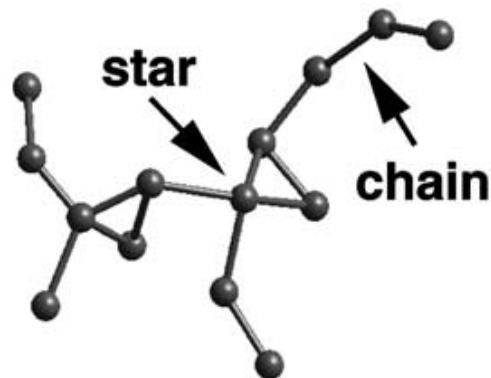
**33% water**

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## **non-percolated water**



**10% water**



**water cluster**

## **Case Study: water in sucrose solution**

*Threshold distance for the percolation : 4 Å*

*As increasing water contents, water connectivity is enhanced. (due to swelling)*

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