Stabilization of $\alpha$-Helices by Dipole–Dipole Interactions within $\alpha$-Helices

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Including solvation effects (in the Poisson–Boltzmann continuum solvent approximation) we report ab initio quantum mechanical calculations (HF/6-31G**) on the conformational energies for adding alanine to the amino or carboxyl terminus of a polyalanine $\alpha$-helix as a function of helix length $N$. We find that extending the length of an $\alpha$-helix increasingly favors the $\alpha$-helix conformation for adding an additional residue, even in hydrophobic environment. Thus, $\alpha$-helix formation is a cooperative process. Using charges from the QM calculations, we find that the electrostatic energy dominates the QM results, showing that this increasing preference for $\alpha$-helix formation results from dipole–dipole interaction within the $\alpha$-helix. These results provide quantitative preferences and insight into the conformational preferences and kinetics of protein folding.

1. Introduction

To carry out directed design of new proteins with designed properties, it is important to understand the determinants of the structure and properties of natural proteins. In particular, we need to understand the relation between the sequence and the kinetics of protein folding to understand how the primary sequence of amino acids influences the native structure of a protein. Hierarchical procedures using the primary sequence of a protein to reduce the number of plausible conformations of a protein are essential to reduce the number of conformations to a level that can be rapidly analyzed by the modern computers and methods. Since 70% of protein structures consist of specific secondary structures (mostly $\alpha$-helix, $\beta$-sheets, and turns), the ability to predict secondary structures is essential to predicting the tertiary structures of proteins, and many methods have been developed starting with the Chou and Fasman analysis of secondary structure preferences. The current state of the art is incorporated in PhD (see also ref 15 for review).

Many good model systems have been developed for understanding the $\alpha$-helix secondary structures of proteins. The formation of the first turn of an $\alpha$-helix has been shown to be rate-determining in the formation of the whole $\alpha$-helices. After formation of this first turn, the growth process of $\alpha$-helix elongation is fast and cooperative, leading to $\alpha$-helix formation in nanosecond time scales.

The parallel alignment of both the amino (NH) and carbonyl (CO) groups of each residue constituting an $\alpha$-helix leads to a net dipole moment (the macrodipole) with the partial positive charge at its N-terminus and the partial negative charge at its C-terminus. The interactions between the dipole moments of the $\alpha$-helix with dipolar or charged groups located at the ends have been studied experimentally, showing that these interactions help stabilize dipolar groups through dipole–dipole interactions and stabilize charged groups through dipole-charge interactions, with the former less screened by solution effects. However, there has been less attention paid to the interactions occurring within the macrodipole of $\alpha$-helices (Figure 1).

Gas-phase quantum mechanical (QM) calculations have suggested that the right-handed $\alpha$-helical conformation is not a stable structure because the dipole moment of each residue is located in an unfavorable orientation with each other. However, we find that including solvation accurately in the QM calculations favors stabilizing the $\alpha$-helical conformation with respect to the $\beta$-sheet conformation.

On the other hand, most $\alpha$-helices found in the X-ray crystal structures of proteins are in hydrophobic regions (even the amphiphilic $\alpha$-helices aggregate in water to avoid exposing the hydrophobic face to solvent). This implies that $\alpha$-helices can form in hydrophobic environments.

To learn how this occurs we carried out QM calculations on polyalanine peptides to study factors stabilizing and determining $\alpha$-helical conformations even in hydrophobic environment. We find that monodipole–macrodipole interactions within an $\alpha$-helix (see Figure 1) increasingly stabilizes longer $\alpha$-helices.

Figure 1. Schematic diagram for the monodipole–macrodipole interactions. The small black arrow indicates the dipole of each alanine monomer (monodipole), the big gray arrow indicates the total dipole moment of the $\alpha$-helix (macrodipole) in which the one alanine at the N-terminus is excluded while the long black arrow indicates the resulting total dipole moment of the $\alpha$-helix. As indicated by the orientation of the dipole moment vector, the N-termini are positive (at the top) while the C-termini are negative (at the bottom). (a) (Ala)$_n$$_N$; a 4-alanine peptide in which all alanines are in the $\alpha$-helical conformations ($\phi = -57^\circ$, $\psi = -47^\circ$), (b) (Ala)$_n$$_Np$ or (Ala)$_n$$_Na$; the same as (Ala)$_n$$_N$ except the alanine at the N-terminus is in its parallel $\beta$-sheet ($\phi = -119^\circ$, $\psi = 113^\circ$) or antiparallel $\beta$-sheet ($\phi = 139^\circ$, $\psi = 135^\circ$) conformation. (c) (Ala)$_n$$_N$; (d) (Ala)$_n$$_Np$ or (Ala)$_n$$_Na$.

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TABLE 1: Geometric Data Parameters Used for the Polyalanine

<table>
<thead>
<tr>
<th>bond</th>
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<th>bond</th>
<th>length (Å)</th>
</tr>
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<tr>
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<td>Cc—N</td>
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<td>N—C(H3)</td>
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<td>Cc—C(H3)</td>
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</tr>
<tr>
<td>Ca—Cc</td>
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<td></td>
</tr>
<tr>
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</tr>
<tr>
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<td>Ca—Cc—O</td>
<td>122.0</td>
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<tr>
<td>Cc—N—H</td>
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<td>Ca—Cc—N</td>
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<tr>
<td>Cc—N—Ca</td>
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<tr>
<td>Cc—N—Cc—Cc</td>
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<td></td>
<td></td>
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</table>

* Indicate two Φ and Ψ torsional angles.

Section 2 discusses the methods and section 3 describes the results. On the basis of these results section 4 discusses the folding mechanism of α-helix formation.

2. Calculation Methods

The calculations considered only polyalanine peptides, CH₃CO—(Ala)ₙ—NH₂CH₃, in which the N- and C-termini were neutralized by adding CH₃CO— and —NH₂CH₃ groups, respectively. This avoids extra charges that might play a role at the amino and carboxyl termini. The notational and geometry information for the polyalanine peptides are shown in Figure 1 and Table 1, respectively.

2.1. QM Calculations. All QM calculations were at the Hartree–Fock (HF) level using the 6-31G** basis for all atoms (using the Jaguar 3.5 quantum chemistry program).32,33 Solvation was included using the Poisson–Boltzmann continuum model (PBQ) with a realistic molecular surface (van der Waals radius plus solvent radius about each atom)34 in Jaguar 3.5 from Schrodinger. We used a dielectric constant for water of 80.37 and a probe radius of 1.4 Å for water. At each iteration, the wave function is calculated self-consistently in the field of the solvent and then the charges (based on the electrostatic potential from the HF wave function) are used to calculate a new reaction field. This process is repeated until convergence. The solvent reaction field is updated at each SCF step.

2.2. Conformational Maps. We examined the dipole–macrodipole interactions between the dipole moment (monodipole) of the alanine at the amino terminus (as a function of conformation) and the macrodipole of the N—1 α-helix residues (Figure 1) using QM with solvation. To study the length dependence of the monodipole–macrodipole interaction within α-helix, we carried out QM calculations for (Ala)ₙ–N, a 4-alanine peptide in which all alanines are in the α-helical conformation except the alanine at the N-terminus can be in any conformation. We also carried out QM calculations for (Ala)ₙ–N, the same as (Ala)ₙ–N except a 7-alanine peptide. To determine the effect of α-helix length on the monodipole–macrodipole interaction, the difference between the QM results for (Ala)ₙ–N and (Ala)ₗ–N were calculated. To extract the pure effect of the three alanines added at the C-terminus of the (Ala)ₙ–N to make (Ala)ₗ–N, all alanines except the one on the amino terminus were kept in the α-helical conformation for all calculations.

The QM calculations were carried out for torsional angles of ϕ = −180° to 0° and ψ = −180° to 180° with increments of 60°. This leads to 24 points. We calculated 16 additional points to improve the contour around the α-helix and β-sheet conformations. Here we considered the torsional angles of ϕ = −30° to −90° and ψ = −150° to −90°, and ϕ = −90° to −150° and ψ = 90° to 150°, respectively. We also considered three additional conformations corresponding to α-helix (ϕ = −57° and ψ = −47°), parallel β-sheet (ϕ = −119° and ψ = 113°), and antiparallel β-sheet (ϕ = −139° and ψ = 135°). For the energy maps (Figures 2 and 3) the geometry of each conformation (Table 1) was created using the amino acid building model from Insight.35 The geometries were not optimized at this point so that we could study the pure effects of the dipole-macrodipole interaction according to the relative orientation of the dipole moment of the added alanine to the macrodipole of the original α-helices.

The same calculations were carried out for monodipole–macrodipole interactions between the alanine at the carboxyl terminus and the macrodipole of the N—1 α-helix residues (Figure 4).

2.3. MM Calculations. To interpret the QM conformational energy surface in terms of electrostatic interactions, we carried out classical electrostatic energy calculations using the ESP derived point charges from the QM calculations. The bonds, angles, torsions, and all the other force field terms were turned off. ESP derived charges are sensitive to conformational changes. We tested the two cases with the two set of ESP derived charges as shown in Table 2: (i) all N alanines in the α-helical conformation and (ii) the N-terminus in the β-sheet conformation but the remaining N—1 residues in the α-helical conformation. We used the MM electrostatic energies to compare with the results of QM calculations (Table 2). (Other details of the MM calculations are in the caption of Table 2.) We found that MM electrostatic energy difference for α-helix versus β-sheet matches well the QM difference.

2.4. Optimized Structures for α-Helix and β-Sheet Amino Terminus. To determine the length dependence of differential energy stabilization for the alanine at the N-terminus (and C-terminus) of an α-helix, we carried out QM calculations for polyalanine peptides for various lengths of α-helices. In these calculations, the geometry was completely optimized quantum mechanically but with the appropriate torsional angle constraints for all residues. The QM calculations were done both in gas phase and solvated in water (Figure 5, Table 3).

3. Results

3.1. Conformational Maps. 3.1.1. QM Results. Figure 2 shows the results of QM calculations for various ϕ and ψ torsional angles of the added alanine at the N-terminus while the structure of the remaining residues is kept fixed in an α-helix. The maps are qualitatively similar to those for the Gly-Ala-Gly tripeptide in our previous calculations (Figure 2 in ref 31), but the depth of the minima and the height of the maxima are different. These results show clearly that adding alanine to
the amino terminus of an α-helix leads to distinct minima at the α-helical and β-sheet conformations.

Figure 2a shows that adding alanine to (Ala)3 in the α-helical conformation is ~3 kcal/mol more stable than adding it in the β-sheet conformation. This differential preference for the α conformation increases as the length of α-helix becomes longer. Thus, Figure 2b shows that adding alanine to (Ala)6 leads to stabilization of α versus β by ~6 kcal/mol. This differential effect is shown in Figure 2c, which shows that adding three alanines [going from (Ala)4 to (Ala)7] increases the stabilization of α by over 3 kcal/mol. Figure 2d shows the magnitude of the dipole moments of (Ala)7 for various conformations. The similarity with Figure 2c suggests that electrostatic interactions within the α-helix are the source of this stabilization. In solution, however, this stabilization decreases substantially because of the screening by the water solvent (Figure 3). Compared to the case of (Ala)4, the larger dipole moment of (Ala)7 leads to larger solvation energy, but this screens the monodipole–macrodipole interaction more effectively.

There are two absolute minima for the conformations of the alanine added at the carboxyl terminus, near (φ = −120° and ψ = 60°) and α-helix. For (Ala)4 the minimum near α-helix conformation has 0.25 kcal/mol lower energy than the one near (φ = 120° and ψ = 60°), which increases to 1.83 kcal/mol for (Ala)7. Unlike at the amino terminus, the β-sheet conformations are not minima at the carboxyl terminus. However, the results (Figure 4) show that the same trend occurs at the carboxyl terminus. Figure 4c shows that adding three alanines [going from (Ala)4 to (Ala)7] increases the stabilization of α versus β by over 4 kcal/mol. The similarity between Figure 4c,d also suggests that electrostatic interactions within the α-helix are the source of this stabilization.

3.1.2. MM Results. To measure the role of electrostatic interactions we carried out MM electrostatic energy calculations on the secondary structures of (Ala)4 and (Ala)7. Table 2 shows...
that the electrostatic energies dominate the conformational preferences. Using QM charges from the \((\phi = -60^\circ)\) conformation, the electrostatic energy difference between \(\alpha\) and \(\beta\) from the MM calculations is comparable (0.5–1.0 kcal/mol larger) to the QM energy. Indeed, the differential stability for \((\text{Ala})_4\) to \((\text{Ala})_7\) is also comparable (0.4–1.3 kcal/mol smaller). This shows that most of the extra stability of adding alanine in the \(\alpha\)-helical conformation rather than in the \(\beta\)-sheet conformation comes from the dipole-macrodipole interaction, as expected. Similar results are obtained using charges for \((\phi = 120^\circ)\) or \((\phi = 60^\circ)\) conformation, supporting this interpretation.

### 3.1.3. Length Dependence of \(\alpha\)-Helix Stability

Fully optimizing these structures (only with the appropriate torsional angle constraints for each residue) with QM leads to the results in Table 3 and Figure 5, which show that stabilization of an \(\alpha\)-helix conformation for alanine at the N-terminus increases with the length of the \(\alpha\)-helix. However, the incremental stabilization (Table 3b) decreases slightly with \(N\) since the distance between dipole moments increases. In solution this decrease in stability is quite strong because of screening by the water solvent.

### Table 2: Comparison of Gas Phase Energies for the Amino Terminus Alanine Having an \(\alpha\)-Helix or \(\beta\)-Sheet Conformation

<table>
<thead>
<tr>
<th>Amino Terminus Alanine Having an (\alpha)-Helix or (\beta)-Sheet Conformation</th>
<th>((\text{Ala})_4_N)</th>
<th>((\text{Ala})_7_N)</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. Absolute Energies</td>
<td></td>
<td></td>
</tr>
<tr>
<td>((\text{Ala})_4_N)</td>
<td>((\text{Ala})_7_N)</td>
<td></td>
</tr>
<tr>
<td>E_(\alpha)</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>E_(\alpha)-p(\beta)</td>
<td>8.00</td>
<td>12.06</td>
</tr>
<tr>
<td>E_(\alpha)-a(\beta)</td>
<td>6.78</td>
<td>9.69</td>
</tr>
<tr>
<td>B. Relative Energies</td>
<td></td>
<td></td>
</tr>
<tr>
<td>((\text{Ala})_4_N)</td>
<td>((\text{Ala})_7_N)</td>
<td></td>
</tr>
<tr>
<td>dE_(\alpha)-p(\beta)</td>
<td>-8.00</td>
<td>-4.40</td>
</tr>
<tr>
<td>dE_(\alpha)-a(\beta)</td>
<td>-6.78</td>
<td>-2.83</td>
</tr>
</tbody>
</table>

\(\alpha\) Table 2a gives the total QM energy but only the electrostatic energy from the MM electrostatic energy calculations. Table 2b gives the difference between \(\alpha\)-helix and \(\beta\)-sheet. Table 2c gives the differential energies between adding a new alanine at the N-terminus using torsional angles of \((\phi = -60^\circ)\) and \((\psi = 60^\circ)\). The MM calculations used QM charges\(^*\) with the alanine at the N-terminus using torsional angles of \((\phi = -120^\circ)\) and \((\psi = 120^\circ)\). The charges are derived based on the electrostatic potential from the HF wave function with the dipole moment constrained to match the QM.

Figure 4. Same as for Figure 2 except at the carboxyl terminus. In (a) for \((\text{Ala})_4\_C\), the energy for the minimum near \(\alpha\)-helix conformation is 0.25 kcal/mol lower than the one near \((\phi = -120^\circ)\) and \((\psi = 60^\circ)\), which increases to 1.83 kcal/mol in (b) for \((\text{Ala})_7\_C\) accounting the effect of three alanines added at the amino terminus in (a).

Figure 5. Differential energies between adding a new alanine at the N-terminus in either the \(\alpha\)-helix or \(\beta\)-sheet conformation (gas phase energy is indicated by solid line, solvation energy by dashed line, and total solution energy by dotted line; these results are also in Table 3). In each case the remaining \(N-1\) alanines have an \(\alpha\)-helix conformation. All results from QM. Each point indicates the energy difference. The filled squares (■) consider the parallel \(\beta\)-sheet \(E\((\text{Ala})_\text{N}\_\alpha\) - \(E\((\text{Ala})_\text{N}\_\beta\)\) while the filled triangles (▲) \(E\((\text{Ala})_\text{N}\_\alpha\) - \(E\((\text{Ala})_\text{N}\_\alpha\_\beta)\)\) consider the antiparallel \(\beta\)-sheet. Starting with \(\# = 3\), we see a trend in which the gas phase energy preferentially stabilizes the \(\alpha\)-helix conformation for the alanine added at the N-terminus. Here solvation retards this stability by an amount that decreases with length.

\(\approx -120^\circ\) and \(\approx 120^\circ\) conformation, supporting this interpretation.
TABLE 3: Differential Energies for Adding a New Alanine at the N Terminus in Either the α-Helix or β-Sheet Conformationa

<table>
<thead>
<tr>
<th>N</th>
<th>δ(α - pβ)</th>
<th>δ(α - aβ)</th>
<th>δ(α - pβ)</th>
<th>δ(α - aβ)</th>
<th>δ(α - pβ)</th>
<th>δ(α - aβ)</th>
<th>total solution energy</th>
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<tr>
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b. Change of Differential Energies (δδN = δS − δrN−1) per Alanine Additiona

<table>
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<tr>
<th>N</th>
<th>δδ(α - pβ)</th>
<th>δδ(α - aβ)</th>
<th>δδ(α - pβ)</th>
<th>δδ(α - aβ)</th>
<th>δδ(α - pβ)</th>
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<th>total solution energy</th>
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<td>6</td>
<td>−0.81</td>
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<tr>
<td>7</td>
<td>−0.61</td>
<td>−0.65</td>
<td>0.37</td>
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<td>0.54</td>
<td>0.55</td>
<td>0.03</td>
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</table>

These results are also in Table 3. All results from QM. Negative δ indicates that the α-helix is more stable. δδ(α - pβ) = E(α) - E(pβ), where the N-terminus alanine has α-helical or parallel β-sheet conformation. δδ(α - aβ) = E(α) - E(aβ), where the N-terminus alanine has α-helical or antiparallel β-sheet conformation. Here a negative number indicates that the α-helix is increasingly stabilized by the increase in length.

change of differential solution energy (between α-helix and β) as the α-helix length increases.

Figure 5 shows that for a single alanine (a dipeptide actually, because of the CH₃CO and NHCH₃ groups added to the N- and C-terminus of an alanine, respectively), the α-helical conformation is 4.6 kcal/mol less stable than the β-sheet structures in gas phase. This energy difference is reduced in water, because the solvation substantially stabilizes the α-helical conformation over the β-sheet conformations. As a result in water the α-helical conformation is 1.6 kcal/mol less stable than the β sheet conformation.

For all peptides studied, the effect of the dipole-macrodipole interaction in solution is smaller than for the gas phase because the screening effects of solvation. However, as the length of α-helices increases, the difference of the differential energies between in the gas phase and in solution decreases for the short length of α-helices (when the number of alanine is less than 5) while it becomes bigger for long α-helices (when the number of alanine is greater than 4).

4. Discussion

It is well-known that α-helices lead to dipole moments along their axes, pointing from the C-termini to the N-termini.23,24 These dipole moments are developed by the appropriate alignment of both the amino and carbonyl groups of each residue in its α-helical conformation, resulting a partial positive charges at the N-terminii and a partial negative charges at the C-terminii of α-helices. Many experimental and theoretical studies have shown both the existence of these α-helix dipole moments and the interactions of this α-helix dipoles with dipolar or charged groups located at the end of the α-helices.29–31 As shown in Table 4 we also find an increased dipole with length in both gas phase and solution.

However, little attention has been paid to the interactions occurring within the alanine dipoles of the α-helix. Our calculations on the polyalanine peptides show that there exist substantial interactions among the dipole moments of each residue with the whole dipole moment of the α-helix. These interactions help the peptides retain the α-helical structure by stabilizing each residue in its α-helical conformation over the β-sheet conformation.

These interactions can be thought of as dipole–dipole interactions between the dipole moment of each residue with the dipole moments of the remaining residues in the α-helices (Figure 1). This picture is oversimplified because the distribution of local dipoles at short distances leads to important multipole–multipole contributions. Hence we refer to them as the monodipole–macrodipole interactions.

To obtain reliable magnitudes for these monodipole–macrodipole interactions, it is necessary to use peptides longer than 4 residues. For the case of two alanines (actually a tripeptide), our results show that there exists a dipole–dipole interaction between the dipole moments of each residue. In gas phase the dipole–dipole interaction stabilizes the (Ala)₂–Nα while it destabilizes (Ala)₂–Npβ and (Ala)₂–Naβ (Table 3). In solution, however, (Ala)₂–Nα does not gainasmuch stabilization as other lengths of α-helices. It seems that the net effect of solvation and screening approaches zero for the case of two alanines.

These results support the conclusion that formation of the first turn of an α-helix is the rate-limiting step.18 Table 3 and Figure 5 suggest that until the first H-bond between alanines of i and i+4 is formed, adding alanine at the amino terminus in the α-helical conformation is less stable than adding it in the β-sheet conformations. As the α-helix length extends, the dipole–macrodipole interaction increasingly favors the alanine addition at the amino terminus in the α-helical conformation as compared to a β-sheet conformation. This is reasonable since increasing the length of the α-helix leads to increasing dipole-macrodipole interactions that stabilizes the whole structure when the alanine at the amino terminus has the α-helical conformation while the dipole-macrodipole interaction becomes worse when the alanine at the amino terminus has the β-sheet conformation (Figure 1).

This explains the cooperative process in forming α-helices.19–21 After forming the first turn of an α-helix, additional residues added to the end of the α-helix stabilize the α-helical conforma-

TABLE 4: Total Dipole Moment (Debye) along Axis of Helix, for the N Terminus α, pβ, or aβ

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<tr>
<th># alanine</th>
<th>α</th>
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<th>aβ</th>
<th>a-pβ</th>
<th>a-aβ</th>
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</table>

# alanine α pβ aβ a-pβ a-aβ

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<th>aβ</th>
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a. Gas Phase

b. Solution Phase

Park and Goddard
Dipole–Dipole Interactions within α-Helix

Our results are consistent with experimental results showing dipole–dipole or charge–dipole interactions between the dipole moment of α-helix and the dipolar or charged group located at the end of the α-helix.25–27 The experimental results also show that the first turn of α-helix contributes most of the interaction (about 80% of the total) with the first two turns contribute 95%.27 Figure 5 shows that in solution phase, protein folding to terminate an α-helix requires a residue (or residues) that breaks the favorable dipole-macrodipole interaction (Figure 1). Thus, the terminal residue must strongly prefer a conformation substantially different than the α-helix (ϕ = −57° and ψ = −47°). To minimize this cost in potential energy there should be a mechanism to neutralize the dipole-macrodipole interaction. Such neutralization could be provided by charged residues, residues with polar groups and residues with high polarizability. The charged residues can neutralize the dipole moment of α-helices by dipole-charge interaction. The polar residues also can neutralize it by dipole–dipole interaction or by making H-bond with any amino or carbonyl groups, which are located at the end of α-helices and therefore are not involved in the i to i + 3 H-bond of α-helices.

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